# Plumcroft Primary School 

Universal High Expectations<br>Knowing every child<br>In pursuit of Excellence



## Calculation policy

## Calculation Policy

This policy contains the key procedures that will be taught within Plumcroft Primary School. It has been written to ensure consistency and progression throughout the school and reflects a whole school agreement.

The ability to calculate mentally lies at the heart of the National Curriculum. The mental methods in the National Curriculum should be taught systematically from Reception upwards and pupils should be given regular opportunities to develop the necessary skills. However mental calculation is not at the exclusion of written recording and should be seen as complementary to and not as separate from it.

In every written method there is an element of mental processing. Sharing written methods with the teacher encourages children to think about the mental strategies that underpin them and develop new, efficient ideas. Therefore written recording both helps children to clarify their thinking and supports and extends the development of more fluent and sophisticated mental strategies.

During their time at Plumcroft, children will be encouraged to see mathematics as both written and spoken language. Teachers should support and guide children through the following important stages:

- Developing the use of pictures and a mixture of words and symbols to represent numerical activities;
- Using standard symbols and conventions;
- Use of jottings to aid a mental strategy;
- Use of pencil and paper procedures;
- Use of a calculator

This policy concentrates on the introduction of standard symbols, the use of the empty number line as a jotting to aid mental calculation and on the introduction of pencil and paper procedures. It is important that children do not abandon jottings and mental methods once pencil and paper procedures are introduced. Therefore children will always be encouraged to look at a calculation/problem and then decide the best method to choose - pictures, mental calculation with or without jottings, structured recording or a calculator. The long-term aim is for our children to be able to select an efficient method of their choice (whether this be mental or written) that is appropriate for a given task. They should be able to do this by asking themselves:

- Can I do this in my head?
- Can I do this in my head using pictures or jottings?
- Do I need to use a formal written procedure?
- Do I need a calculator?


## Oral and mental work in mathematics

Most lessons will begin with oral work and mental calculation ( $5-10 \mathrm{mins}$ ), where children rehearse, strengthen and develop mental and oral skills. It is important that children have sufficient opportunity to consolidate the mathematics teaching they have received. During the main part of the lesson children should be able to access previous calculation strategies and apply them to new situations and questions. Eg encourage the use of known mental facts and times tables.

## Calculators

The use of calculators is no longer an emphasis in the National curriculum, however the children still need to have the opportunity to use them. This is so that they can develop their ability to organise and sequence calculations appropriately. Some lessons may focus on the children's understanding of the process rather than the specific calculation technique.

## Calculation in EYFS

The 'development matters' states that by the end of Nursery children should :

- know that numbers identify how many is in a set
- compare two groups of objects, saying when they have the same number
- show an interest in number problems
- separate a group of 3 and 4 objects, and begin to recognise the total is still the same
by the end of Reception children should :
- Find one more or one less from a given quantity to 20
- add and subtract two single digit numbers using objects, counting on and back to find the answer
- solve mathematical problems, including doubling, halving and sharing


## Stages in counting

All children go through these stages in counting. Generally, they should be secure with them by the end of Year R.

1. Stable order (knowing numbers come in an order)
2. One to one correspondence (touching and counting)
3. Cardinal (knowing last number is the total)
4. Order irrelevance (doesn't matter how you count the total will be the same)
5. Abstraction (being able to count without seeing/touching items)

By the end of Year R children should also be able to:

- Subitise (know number of dots on dice or dominoes without counting)
- Know about the numbers to 10 , for example, 9 is made up of 1 and 8,2 and 7 etc., it is greater than 4, less than 10 (Numicon is great for this)

- Recognise and begin to write numerals


## Key mental calculation strategies

It is important to spend time developing mental calculation strategies so that children have a bank of them to use when calculating. Often a calculation can be answered more efficiently using these and yet most children in KS2 will use a written method. Spend a week or maybe two developing these before working on written methods.

## Some of these are started in EYFS and Year 1 and developed in subsequent years. They include:

From Year R:

- Partition and recombine one number to 20, e.g. $14=10+4$
- Doubles and near doubles, e.g. $6+6=12,25+26=$ double 25 add 1
- Use number pairs to 10 and 100, e.g. $3+7=10,40+60=100,25+75=100,63+37=100$
- Counting on to subtract numbers close together, e.g. $26-17:+3+6=9,2136-1989:+11+136=147$

Keep practising and developing the above. Additional strategies from Year 1:

- Adding near multiples of ten and adjusting,
e.g. $145+199=145+200-1=344,1587+1997=1587+2000-3=3584$
- Sequencing,
e.g. $256+153=256+100+50+3=409$
- Using patterns of similar calculations, e.g. $136+45=181,146+45=191,156+45=201$
- Using known number facts,
e.g. $6 \times 7=42,6 \times 70=420,6 \times 35=210$
- Bridging though ten, hundred, tenth,
e.g. $26+15=30+11=41,125+76=130+71=201$
- Use relationships between operations,
e.g. $4 \times 5=20,5 \times 4=20,20 \div 5=4,20 \div 4=5$

Keep practising and developing the above. Additional strategies from Year 3:

- Regrouping for division,
e.g. $132 \div 3: 120 \div 3=40$ and $12 \div 3=4$
- $x 4$ by doubling and doubling again,
e.g. $36 \times 4=72 \times 2=144$
- $x 5$ by $x 10$ and halving or vice versa,
e.g. $346 \times 5=3460 \div 2$ or $173 \times 10=1730$
- x20 by x10 and doubling,
e.g. $427 \times 20=4270 \times 2=8540$
- $x 15$ by $x 10$, halve and ad, e.g. $135 \times 15: 1350+675=2025$
- $\div 4$ by halving and halving,
e.g. $120 \div 4=60 \div 2=30$
- $\div 5$ by dividing by 10 and doubling,
e.g. $375 \div 5=37.5 \times 2=75$
- $\div 20$ by dividing by 10 and halving, e.g. $246 \div 20=24.6 \div 2=12.3$

Models and images for mental calculation strategies that children may find helpful.


Partitioning for sequencing
$48+33$
V高
$30 \quad 3=78+3=81 \quad 48+30+3=78+3=81$


Tens frames for number pairs to $1,10,100$, multiplication

represents 10 , show me the frame that goes with
to make 10. What calculations can we make? $7+3=10$ and $3+7=10$ because addition is commutative.

What if represents 100 ?
 represents 1 ? 0.1 ? This is a good activity for number facts.

represents 40 , show me 32 . What calculations can we make? $8 \times 4=32,4 \times 8=32$ because multiplication is commutative.

If
 represents 90, show me 108 and so. This is a good way to rehearse multiplication facts.

Multiplication grids to highlight the commutative property of multiplication - we only need to learn half the facts, because in learning one we know two, e.g. if we know $9 \times 4=36$, we also know $4 \times 9=$ 36.

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 2 |  | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 |
| 3 |  |  | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 | 33 | 36 |
| 4 |  |  |  | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 | 48 |
| 5 |  |  |  |  | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 |
| 6 |  |  |  |  |  | 36 | 42 | 48 | 54 | 60 | 66 | 72 |
| 7 |  |  |  |  |  |  | 49 | 56 | 63 | 70 | 77 | 84 |
| 8 |  |  |  |  |  |  |  | 64 | 72 | 80 | 88 | 96 |
| 9 |  |  |  |  |  |  |  |  | 81 | 90 | 99 | 108 |
| 10 |  |  |  |  |  |  |  |  |  | 100 | 110 | 120 |
| 11 |  |  |  |  |  |  |  |  |  |  | 121 | 132 |
| 12 |  |  |  |  |  |  |  |  |  |  |  | 144 |

Focus on square numbers, learn these facts and link in with areas of squares - practically. Teach 3 s and $6 s$ together, $4 s$ and $8 s$ together, $6 s$ and 12 s together because one is double the other.

## Place value

- Positional: the quantities represented by the individual digits are determined by the positions that they hold in the whole numeral. The value given to a digit is according to the position in a number
- Base 10: the value of the position increases in powers of 10
- Multiplicative: the value of an individual digit is found by multiplying the face value of the digit by the value assigned to its position
- Additive: the quantity represented by the whole numeral is the sum of the values represented by the individual digits
For example:

| 1000 | 100 | 10 | 1 |
| :---: | :---: | :---: | :---: |
| 6 | 8 | 3 | 7 |

Positional: 6 is in the 1000's position, 8 in the hundreds, 3 in the tens and 7 in the ones Multipicative: because 6 is in the 1000 's position it is multipled by 1000 to give its value, 8 is multiplied by 100,3 by 10 and 7 by one to give their values.
Additive: add all the numbers together to give the total $6000+800+30+7=6837$
Base 10: if 37 is multipled by 10, 3 tens becomes 3 hundreds, 7 ones become 7 tens and a place holder is placed in the ones position: 370

$$
6 \longdiv { 1 2 5 6 }
$$

The children need to be able to partition numbers in different ways to help understanding and also to encourage mental calculation strategies:

- Partition all pairs of numbers for all numbers to 20 , e.g. $1+4=5,2+3=5,3+2=5$
- Partition 2-, 3- etc. digit numbers in different ways, e.g. 57: $50+7,40+17,30+27,20+17$, $10+7$


## Equals sign

The equals sign is not an indication of an answer. It is a sign of equivalence - the same as.
Year 1: $2+3=1+\square$

Year 5: $23+\mathrm{y}=35$. Take 23 away from both sides, $\mathrm{y}=12$
Year 6: $2 \mathrm{y}+36=40$. Take 36 away from both sides, $2 \mathrm{y}=4$. Divide both sides by $2, \mathrm{y}=2$

## Greater than and less than

Be mathematical when teaching this (no crocodiles)
Show these symbols plus equals like this (good to have on the wall):

$2<4$

$4>2$

$2+2=4$

$2=4-2$

## Addition and subtraction

## National Curriculum requirements

## Year 1

Add and subtract one-digit and two-digit numbers to 20, including zero using concrete objects, pictorial representations and mentally
Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7=$ 回-9

## Year 2

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including:

* a two-digit number and ones
* a two-digit number and tens
* two, two-digit numbers
* adding three one-digit numbers

Solve problems with addition and subtraction:

* using concrete objects and pictorial representations, including those involving numbers, quantities and measures
* applying their increasing knowledge of mental and written methods

Solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change (copied from Measurement)

## Year 3

Add and subtract numbers mentally, including:

* a three-digit number and ones
* a three-digit number and tens
* a three-digit number and hundreds

Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction

## Year 4

Add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate
Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why

## Year 5

Add and subtract numbers mentally with increasingly large numbers
Add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)
Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

## Year 6

Perform mental calculations, including with mixed operations and large numbers
Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
Solve problems involving addition, subtraction, multiplication and division

## Structures for addition

## Aggregation (counting all)

5

7

12


## Augmentation (adding on to a set)

7


Vocabulary: augend add addend equals sum, commutative

## Progression towards the written method

Year R: Use counters, bead strings, any 'stuff' and progress to Numicon to encourage counting on from one number to find the sum of quantities to 10 and, if appropriate, to 20.

Year 1: Continue using Numicon, finding the two numbers putting them together and finding the sum without counting everything to 20 and, if appropriate, to 50 .

Combine tens and ones using Dienes or bundles of straws and write number statements/draw pictures to show what they have done. Towards the end of Year 1 explore exchange.

Year 2: Continue combining Dienes to make sums up to 100 , including exchange. Writing number statements/drawing pictures to show what they have done.

Towards end of the year introduce vertical partitioning to prepare children for Year 3. (expanded method - start from right)

48
$+\underline{33}$
11
$\underline{70}$
81

Year 3 and above: Use of manipulatives to lead to the written method. Important to explore why they need to begin with the least significant number.

## Be careful to use 3-digit examples that cannot be answered using a mental method.

$248 \quad$ leading to 248 with manipulatives
$\begin{array}{r}+139 \\ \hline\end{array}$
17
$\begin{array}{r}+139 \\ \hline\end{array}$
387
70
300
387


What's the same? What's different?


Every time new numbers are introduced, e.g. thousands, decimal places, use manipulatives first so children can see that the process is essentially the same.

## Structures for subtraction

Subtraction (take-away)


Difference (comparison model)


Reduction (more abstract: temperature, speed)

Progression towards the written method
Vocabulary: minuend subtract subtrahend equals difference
Year R: Use counters, bead strings, any 'stuff' to find the difference between quantities to 10 and, if appropriate, to 20.

Year 1: Continue using the manipulatives from Year $R$ and also Numicon, to find the difference between quantities to 20 and, if appropriate, to 50 .

Make a number using Dienes or bundles of straws and subtract a smaller number. Write number statements/draw pictures to show what they have done. Towards the end of Year 1 explore exchange.

Year 2: Continue using Dienes to find differences between quantities to 100, including exchange. Writing number statements/drawing pictures to show what they have done.


Exchange one 10 for 10 ones in order to take away 7


Year 3 and above: Use of manipulatives to lead to the written method by the end of Year 3, beginning of Year 4.

## Be careful to use 3-digit examples that cannot be answered using a mental method.

Use of manipulatives to lead to compact method:


Written method: decimals (with manipulatives first)


## Multiplication and division

## National Curriculum requirements

## Year 1

Count in multiples of twos, fives and tens (copied from Number and Place Value)

## Year 2

Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division ( $\div$ ) and equals (=) signs

## Year 3

Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

## Year 4

Use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers
Multiply two-digit and three-digit numbers by a one-digit number using formal written layout

## Year 5

Multiply and divide numbers mentally drawing upon known facts
Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers
Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context

## Year 6

Perform mental calculations, including with mixed operations and large numbers
Solve problems involving addition, subtraction, multiplication and division
Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication
Divide numbers up to 4-digits by a two-digit whole number using the formal written method of short division where appropriate for the context divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context Use written division methods in cases where the answer has up to two decimal places (copied from Fractions (including decimals)

## Structures of multiplication

Grouping (repeated addition)
Scaling (2, 3, 4 etc. times as many)

## Progression towards the written method

Vocabulary: multiplicand multiplied by multiplier equals product, commutative
Year R: Use counters, bead strings, any 'stuff' to groups of quantities to 10 and, if appropriate, to 20.
Year 1: Continue using the manipulatives from Year $R$ and also Numicon, to find groups of quantities, e.g. 2, 5 and 10 to 20 and, if appropriate 50.


4 groups of $3=3$ four times $=3 \times 4$
Bead strings

Set counters out as arrays and explore commutativity and early inverse by taking groups away.
Arrays


Year 2: Continue as in Year 1, focussing on arrays, include multiplying by 3 and writing the commutative number statements.

## Fingers



12


Year 3 and above: Use arrays and link to the grid methods, beginning with 2-digit multiplicands. Be sure to use multipliers that do not lend themselves to a mental method, e.g. 2, 4, 5, 10.
These multipliers are suitable: $3,6,7,8$ and 9 .
Arrays to support the grid method

3


|  | 10 | 8 |
| :---: | :---: | :---: |
| 3 | 30 | 24 |

$18 \times 3=54$


|  | 200 | 50 | 2 |
| ---: | ---: | ---: | ---: |
| 6 | 1200 | 300 | 12 |$=1512$


| Or... | leading to written method |
| :--- | :---: |
| 252 | 252 |
| $\times 6$ | $\frac{\times 6}{1512}$ |
| 12 | $\frac{1}{31}$ |
| 300 |  |
| 1200 |  |
| 1512 |  |

Long multiplication begins in Year 5:


Also use Dienes and place value counters to demonstrate this

|  | 10 | 8 |  |
| :---: | :---: | :---: | :---: |
| 10 | 100 | 80 | 180 |
| 3 | 30 | 24 | 54 |
|  |  | Total: | 234 |

## Leading to written method:

| 18 | or... |  |  |
| :---: | :---: | :---: | :---: |
| X 13 | 18 | 18 | 180 |
| 54 | +10 | x 3 | $\begin{array}{r}\text { + } 54 \\ \hline\end{array}$ |
| 180 | $\underline{180}$ | 54 | 203 |
| 234 |  |  |  |

Written method: decimals


|  | 100 | 40 | 5 | .3 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 400 | 160 | 20 | 12 | 180 |
| 3 | 30 | 24 |  | 54 |  |
|  |  | Total: |  |  | 234 |

145.3
$\begin{array}{r}14 \\ \hline\end{array}$
581.2

111

## Structures for division

Grouping (repeated subtraction)
Scaling (a third, quarter, fifth etc. of the size)
Sharing (best linked to fractions)

## Progression towards the written method

Vocabulary: dividend, divisor, quotient, division bracket
Year R: Use counters, bead strings, any 'stuff' to make quantities to 10 , then20 into groups of $2 \mathrm{~s}, 5 \mathrm{~s}$ and 10s.

Year 1: Continue using the manipulatives from Year R and also Numicon, to find how many groups they can make out of quantities, to 20 and, if appropriate 50 .
$12 \div 3$
How many groups of 3 in 12?

Bead strings



Set counters out as arrays and explore taking groups away.

Arrays


Year 2: Continue as in Year 1, focussing on arrays and working out division calculations by counting in step on fingers.

Fingers


Year 3 and above: Use arrays and then move towards the written method using manipulatives.

## Arrays




Introducing the conceptual variation of the written method with division bracket.

$$
7 \longdiv { 5 6 }
$$



7
$8 \longdiv { 5 6 }$


## Written method

## $133 \div 6$

Important to let the children use manipulatives such as place value counters to explore exchange:


You cannot take 6 groups of 100 away from the one 100
Exchange the 100 for 10 tens so you have 13 tens
$6 \longdiv { x ^ { 1 } 3 3 }$

You can now take two groups of 6 tens
$6 \longdiv { x ^ { 1 } 3 3 }$

One groups of ten will be left. This is exchanged for 10 ones. You now have 13 ones.
$6 \longdiv { x ^ { 1 } B ^ { 1 3 } 3 }$

You can take another two groups of 6 ones from the 13 leaving a remainder of 1
$6 \longdiv { x ^ { 1 } \beta ^ { 1 3 } 3 } { } ^ { \frac { 1 } { 6 } }$

## Written method: decimals (with manipulatives first)

## $73.2 \div 6$

Important to let the children use manipulatives such as place value counters to explore exchange:

You can take one group of six 10s away from the seven 10s. There will be one hundred left Exchange the 10 for 10 ones so you have 13 ones
$6 \longdiv { 7 ^ { 1 3 } 3 . 2 }$

You can now take two groups of 6 tens
$6 \longdiv { 1 2 }$


One will be left. This is exchanged for 10 tenths. You now have 12 tenths.
12.2
$\begin{array}{r}7^{1} \not 2 .^{12} 2\end{array}$

You can take two groups of 6 tenths
$6 \longdiv { 1 2 . 2 }$


Numberlines can be used as an introduction to chunking. Jumping up in lots of the divisor.

Long division appears in Year 6 (chunking method = counting up in multiples of the divisor)
$\mathbf{4 6 2 0} \div \mathbf{2 0}$
$100 \times 20=2000$
$100 \times 20=\underline{2000}$
4000
$10 \times 20=\underline{200}$
4200
$10 \times 20=\underline{200}$
4400
$10 \times 20=\underline{200}$
4600
$1 \times 20=\quad 20$
$4620=231$ (lots of 20)

## The bar model

This visual representation helps children make sense of problems. It needs to begin in EYFS (practically and visually) then developed throughout the school. Use manipulatives for this whenever the children want to. Develop the drawings from these. Cuisenaire and double sided counters are good for this.

EYFS:
There are 3 footballs in the red basket and 2 footballs in the blue basket.
How many footballs are there altogether?


Peter has 3 marbles.
Harry gives Peter 1 more marble.
How many marbles does Peter have now?


Peter has 5 pencils and 3 erasers.
How many more pencils than erasers does he have?


Visual to

Larger Quantity


Abstract

Year 1 upwards:

| 10 |  |
| :---: | :---: |
| 4 |  |

This leads to an abstract model which helps with links between addition and subtraction

| $a$ |  |  |
| :---: | :---: | :---: |
| $b$ | $c$ |  |$\quad$| $a=b+c$ | $a=c+b$ |
| :--- | :--- |
| $b=a-c$ | $c=a-b$ |

This can then help the children solve, for example, missing number problems:

$$
45+?=93, ?-62=13,146-?=79, ?+82=147
$$

Peter has 4 books.
Harry has three times as many books as Peter. How many more books has Harry?


Sam had 5 times as many marbles as Tom. If Sam gives 26 marbles to Tom, the two friends will have exactly the same amount. How many marbles do they have altogether?


If the children had been proficient using this model, they would have found these 'Level 5' SATs questions simple:

24
In a class, 18 of the children are girls.
A quarter of the children in the class are boys.


They would have been able to attempt this level 6 question

4
Two numbers are in the ratio 4:5
One of the numbers is 60

There are two possible values for the other number.
What are the two possible values?


And questions like these:
A shop keeper sold $1 / 3$ of his balloons in the afternoon and $2 / 5$ of the remainder in the evening. If he had 150 balloons left, find the number of balloons he had at first?

Iqbal and Sofia have $£ 680$ altogether. If Iqbal spends
$\frac{2}{5}$ of her money and Sofia spends $£ 80$, then they will have an equal amount of money left. How much money did Sofia have at first?

Mr Yap had a length of rope. He used $1 / 4$ of it to tie some boxes together. He then used 5/9 of the remainder to make a skipping rope for his daughter. 120 cm of rope were left. What was the length of rope used to tie the boxes together?

Michelle prepared a mixture of apple, carrot and celery juices. $1 / 3$ of the mixture was apple juice and $2 / 5$ of the remainder was celery juice. 315 ml of the mixture was celery juice. What volume of the mixture was carrot juice?

- Number lines : addition to be recorded on top of line, subtraction below line
- Column addition/subtraction : always start on right and move left (even with expanded methods as we do not want to unteach/change things later that might confuse when children move on to a new method)
- Column subtraction: Use the word 'exchange' rather than 'borrow'
- Column methods: Encourage the use of place holders to ensure the children have the same number of digits in both numbers that they are adding or subtracting, to avoid recording errors
- Teach BODMAS year 5
- Number target cards to be used in year 2 and 3 ( and introduced in year 1 to those who are ready) to secure number skills
- Ensure when we are $x$ and dividing by $10,100,1000$ we talk about moving the digits not the decimal point. Likewise we are not just 'adding zeros on the end'
- Column addition: when carrying up into the next column, record the number being carried up small, and through the bottom line in the answer box
- Column multiplication: if multiplying by 24 , once you have multiplied everything by the 4, put a line through it. Remember to place a zero in the next row down before multiplying by the 2.
- Short division: any number carried over to the next column should be recorded small and to the top left of the number it is being carried over to.
- When you are introducing a new calculation the children must understand the place valuie needed first
- They need to see the transition from one method into the next and how it is 'the same' but more advanced or more efficient. This understanding is important for them to remember and have confidence in the new method.

New curriculum - calculating fractions (to be introduced in year 5)
Addition: Add the numerators, the denominators stay the same : $2 / 5+2 / 5=4 / 5$

Progression: (different denominators) find a common denominator first
$2 / 5+3 / 10 \quad 4 / 10+3 / 10=7 / 10$

Subtraction: subtract the numerator, the denominator stays the same : 6/9-2/9 = 4/9 Progression: (different denominators) find a common denominator first
$7 / 8-3 / 16=\quad 14 / 16-3 / 16=11 / 16$

Further progression: (mixed numbers)
$11 / 4-3 / 4$ (turn the mixed number into an improper fraction first)
$5 / 4-3 / 4=2 / 4$

Further progression: (different denominators) find common denominator first

Multiplication: multiply the numerators, multiply the denominators
$2 / 5 \times 2 / 5=4 / 25$

Progression: fraction x whole number
$1 / 3 \times 150$ same as $1 / 3$ OF 150 so divide by denominator x by numerator

150 div by $3=50, \times 1=50$

Progression: mixed number x whole number

As above, can partition the mixed number into a whole number and a fraction
$21 / 2 \times 17 \quad 2 \times 17=34 \quad 1 / 2 \times 17 \quad(17$ div by 2$)=8.5$
$34+8.5=42.5$

Division: (for year 6 they only need to divide by a whole number)
$4 / 6$ div by 2 (divide numerator by 2, denominator stays same)
$4 / 6$ div by $2=2 / 6$

Note: do not only teach children the mechanical calculations for working with fractions, ask them to verbalise what they are trying to find out, change the $x$ to 'lots of' to see if they can visualise what they are trying to find out. Make sure they understand that $x 1 / 2$ means $1 / 2$ a lot of etc

